## SCIENCE 1206 UNIT 3: MOTION WORKSHEET #9: MATHEMATICAL RELATIONSHIPS



Interpolation:	finding values between measured points		
Extrapolation:	finding values beyond measured points by extending the graph using a dotted line		
Slope :	Refers to the steepness of a line. It represents a mathematical relationship between the variables, and can be calculated by		

Slope	=	<u>Rise</u> = Run	$\frac{y_2 - y_1}{x_2 - x_1} =$	$\frac{\Delta y}{\Delta x}$

## Types of Relationships

- 1. Direct Proportionality occurs when a change in the independent variable causes a corresponding change in the dependent variable, as in the case of the straight line graph.
- Written mathematically as  $y \alpha x$
- spoken as "y is directly proportional to x"



- 2. Inverse (indirect) Proportionality occurs when a change in the independent variable causes an inverse (or reciprocal) change in the dependent variable
- Written mathematically as  $y \alpha 1/x$
- spoken as "y is inversely proportional to x"



When a line of best fit is a straight line, there is a simple relationship between the two variables. This relationship can be represented by a general mathematical equation:

 $\mathbf{y} = \mathbf{m}\mathbf{x} + \mathbf{b}$ 

where :

- y is the dependent variable = DISTANCE
- x is the independent variable = TIME
- m is the slope (steepness) of the line
- b is the y-intercept (i.e. where the graph crosses the y-axis)

PART A: Multiple Choice

- 1. Find the slope of the line that passes through the points (2,7) and (2,-6).
  - (A)
  - (B) 0
  - (C) undefined

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(D) -1

2. Find the slope of the line that passes through the points (4,10) and (2,10).

- (A) 1 (B) 0
- (C) undefined
- (D) -1
- 3. Find the slope of the line that (10, -1) contains and (-8, 6)

(A) 
$$\frac{2}{5}$$
  
(B)  $-\frac{7}{18}$   
(C)  $-\frac{18}{7}$   
(D)  $\frac{5}{2}$ 

- 4. Find the slope of the line that contains (2, -10) and (-4, 2)
  - (A)  $\frac{1}{4}$ (B) -2
  - (C) 4
  - (D)  $-\frac{1}{2}$

5. Which of the following describes the y-intercept?

- (A) Point where the graph crosses the x- axis
- (B) Point where the graph crosses the y- axis
- (C) Point where the graph is at the vertex
- (D) The graph is undefined

6. Find the slope of the line that contains (-2,-2) and (-10, -9)

(A) 
$$\frac{8}{7}$$
  
(B)  $\frac{11}{12}$   
(C)  $\frac{12}{11}$   
(D)  $\frac{7}{8}$ 

Use the graph below to answer questions 7-12



- 7. Which term would describe the mathematics relationship shown by the graph?
  - (A) 0
  - (B) Directly proportional
  - (C) Inversely proportional
  - (D) Undefined
- 8. What is the slope of the graph?
  - (A) 0
  - (B) 0.5
  - (C) 1.0
  - (D) 2.0
- 9. What are the units of the slope?
  - (A) m (B) m/s
  - $(C) \qquad s$
  - (D) s/m
- 10 What is the y- intercept of the graph?
  - (A) -1
  - (B) 0
  - (C) 1
  - (D) 2

- 11. Using interpolation, what is the distance at 4.0 s?
  - (A) 0 m (B)
  - 1.0 m (C) 3.0 m
  - 4.0 m
  - (D)
- Using interpolation, at what time did the object travel 4.5 m? 12.
  - (A) 0 s
  - 4.4 s (B)
  - 7.0 s (C)
  - (D) 10. s

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- 13. Which of the following lines has a negative slope?
  - (A)
  - (B)
  - (C) (D) 3 4



- 14. Which of the following lines has the greatest slope?
  - (A) 1
  - 2 (B) (C)
  - 3 4 (D)



Use the graph below to answer questions 15-18



- 15. Which term would describe the mathematics relationship shown by the graph?
  - (A) 0
  - (B) Directly proportional
  - (C) Inversely proportional
  - (D) Undefined
- 16. What is the slope of the graph?
  - (A) -2.0
  - (B) -1.0
  - (C) 0
  - (D) 1.0
- 17. What are the units of the slope?
  - (A) m
  - (B) m/s
  - (C) m/s/s
  - (D) s/m
- 18 What is the y- intercept of the graph?
  - (A) 0
  - (B) 50
  - (C) 100
  - (D) 150
- 19. What is velocity of the car at 20 s?
  - (A) 0 m/s
  - (B) 30 m/s
  - (C) 40 m/s
  - (D) 50 m/s
- 20. Which of the following best describes the slope of a line?
  - (A) It is always equal to zero
  - (B) It is always undefined
  - (C) It is constant for every point on the graph
  - (D) It changes for every point on the graph